

Trans-dimensional Random Fields (TDRF) for Language Modeling

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State-of-the-art LMs – Review

- Dominant: Conditional approach

$$p(x_1, x_2, \dots, x_l) = \prod_{i=1}^l p(x_i | x_1, \dots, x_{i-1})$$

- N-gram LMs

- Neural network LMs

$$p(x_i = k | x_1, \dots, x_{i-1}) \approx \frac{w_k^T \phi[x_1, \dots, x_{i-1}]}{\sum_{k=1}^V w_k^T \phi[x_1, \dots, x_{i-1}]}, \quad w_k \in R^h$$

- ⊗ Computational expensive in both training and testing¹
e.g. lexicon size $V = 10k \sim 100k$, embedding dim $h = 250$

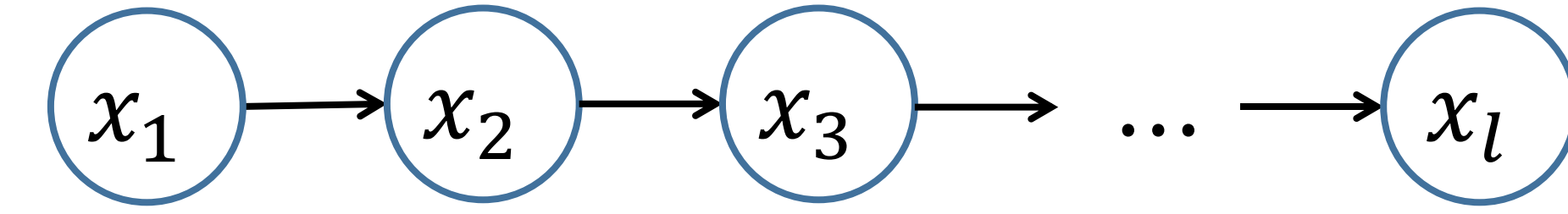
¹ Partly alleviated by using un-normalized models, e.g. through noise contrastive estimation training.

TDRF LMs – Motivation

$$p(x_1, x_2, \dots, x_l) = ?$$

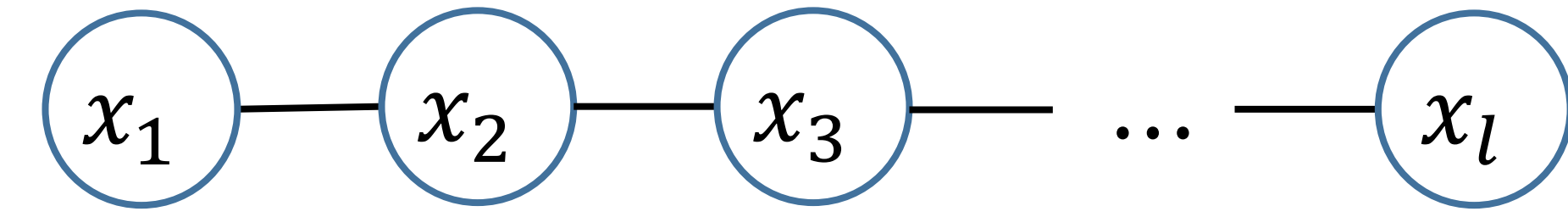
Dominant:

Conditional approach / Directed



Alternative:

Random field approach / Undirected



⊗ Model training is difficult.

⊙ Capture bidirectional context for language cognition.

The cat is on the table.

The cat is in the house.

⊙ Breakthrough in training with a number of innovations

Fixed-dim (e.g. image) -> Trans-dim (sequential modeling)

TDRF LMs – Model Definition

- Features $(f_i, i = 1, 2, \dots, F)$ can be defined flexibly.
- Each feature brings a contribution to the sentence probability.

$$p(x; \lambda) = \frac{1}{Z(\lambda)} \exp\left(\sum_{i=1}^F \lambda_i f_i(x)\right), \quad x \triangleq (x_1, x_2, \dots, x_l)$$

$$f_i(x) = \begin{cases} 1, & \text{'meeting on DAY-OF-WEEK' appears in } x \Rightarrow \lambda_i \text{ is activated} \\ 0, & \text{Otherwise} \Rightarrow \lambda_i \text{ is removed} \end{cases}$$

⊙ More flexible features, beyond the n-gram features, can be well supported in TDRF LMs.

⊙ Computational efficient in computing sentence probability for testing.

Jelinek 1995: put language back into language modeling

WSME vs TDRF

- Whole-sentence maximum entropy (WSME) (Rosenfeld, Chen, Zhu 2001)

$$p(l, x^l; \lambda) = \frac{1}{Z(\lambda)} \exp[\lambda^T f(x^l)], \quad x \triangleq (l, x^l), \quad x^l \triangleq (x_1, x_2, \dots, x_l)$$

$$= \frac{Z_l(\lambda)}{Z(\lambda)} \cdot \frac{1}{Z_l(\lambda)} \cdot \exp[\lambda^T f(x^l)], \quad Z_l(\lambda) = \sum_{x^l} \exp[\lambda^T f(x^l)]$$

A mixture distribution with unknown weights, which differ from each other greatly, e.g. 10^{40} !

Poor sampling → poor estimation of gradient → poor fitting

- Trans-dimensional RF (TDRF) model

$$p(l, x^l; \lambda) = \pi_l \cdot \frac{1}{Z_l(\lambda)} \cdot \exp[\lambda^T f(x^l)], \quad l = 1, \dots, m$$

Empirical length probabilities in the training data

Serve as a control device to improve sampling from multiple distributions!

TDRF LMs – Model Estimation

- Maximum-likelihood training

$$\frac{\partial \text{LogLikelihood}}{\partial \lambda} = E_{\tilde{p}(x)}[f_i(x)] - E_{p(x; \lambda)}[f_i(x)] = 0$$

Expectation under empirical distribution $\tilde{p}(x)$

Expectation under model distribution $p(x; \lambda)$

- Consider $p(l, x^l; \lambda, \zeta) \propto \pi_l \cdot \frac{1}{e^{\zeta_l}} \cdot \exp[\lambda^T f(x^l)]$

where ζ_l is hypothesized values of the true $\zeta_l^*(\lambda) = \log Z_l(\lambda)$.

The marginal probability of length l is: $p(l; \lambda, \zeta) = \frac{\pi_l e^{-\zeta_l + \zeta_l^*(\lambda)}}{\sum_j \pi_j e^{-\zeta_j + \zeta_j^*(\lambda)}}$

- Joint SA is used to find $\zeta_l^* = \zeta_l^*(\lambda^*)$ and λ^* that solves

$$\begin{cases} \pi_l = p(l; \lambda, \zeta), & l = 1, \dots, m \\ 0 = E_{\tilde{p}(x)}[f_i(x)] - E_{p(l, x^l; \lambda, \zeta)}[f_i(x)] \end{cases}$$

Experiments

LM Training — Penn Treebank portion of WSJ corpus

Test speech — WSJ'92 set, by rescoring of 1000-best lists

Type	Features	WER	PPL (\pm std. dev.)	#feat
KN4		8.71	295.41	1.6M
RNN		7.96	256.15	5.1M
WSMEs (200c)				
w+c+ws+cs		8.87	$\approx 2.8 \times 10^{12}$	5.2M
w+c+ws+cs+cpw		8.82	$\approx 6.7 \times 10^{12}$	6.4M
TDRFs (100c)				
w+c	$(w_{-3}w_0)(w_{-3}w_{-2}w_0)$ $(w_{-3}w_{-1}w_0)(w_{-2}w_0)$	8.56	268.25 \pm 3.52	2.2M
w+c+ws+cs		8.16	265.81 \pm 4.30	4.5M
w+c+ws+cs+cpw		8.05	265.63 \pm 7.93	5.6M
w+c+ws+cs+wsh+csh		8.03	276.90 \pm 5.00	5.2M
TDRFs (200c)				
w+c	$(w_{-4}w_0)(w_{-5}w_0)$	8.46	257.78 \pm 3.13	2.5M
w+c+ws+cs		8.05	257.80 \pm 4.29	5.2M
w+c+ws+cs+cpw		7.92	264.86 \pm 8.55	6.4M
w+c+ws+cs+wsh+csh		7.94	266.42 \pm 7.48	5.9M
TDRFs (500c)				
w+c		8.72	261.02 \pm 2.94	2.8M
w+c+ws+cs		8.29	266.34 \pm 6.13	5.9M

Comparison	Computation efficient in training	Computation efficient in testing	Bidirectional context	Flexible features	Performance
N-gram LMs	✓	✓	✗	✗	✗
Neural network LMs	✗	✗	✗	✓	✓
TDRF LMs	✗	✓	✓	✓	✓